

# SUPPLEMENTARY MATERIAL for Three-Outcome Dual-Criterion Randomized Phase II Clinical Trial Design

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## 1 3-by-2 design

The TDR design can be extended to the 3-by-2 decision boundaries to allow finer control of inconclusive regions. The difference between a 3-by-2 design and a 2-by-2 design is that two difference boundaries, a lower boundary  $r$  and an upper boundary  $s$ , are employed to define an inconclusive region where the difference in treatment and control responses is borderline. Therefore, the definitions of  $\alpha, \beta, \eta$ , and  $\gamma$  change accordingly as below:

$$\begin{aligned}
 \alpha &= \sum_{D_1 \cap D_3} B(y_E, n_E, p_E | H_0) B(y_C, n_C, p_C | H_0), \\
 \beta &= \sum_{(D'_1 \cap D'_3) \cup D_2} B(y_E, n_E, p_E | H_a) B(y_C, n_C, p_C | H_a), \\
 \eta &= \sum_{((D'_1 \cap D'_2) \cap D_3) \cup (D_1 \cap D'_3)} B(y_E, n_E, p_E | H_0) B(y_C, n_C, p_C | H_0), \\
 \gamma &= \sum_{((D'_1 \cap D'_2) \cap D_3) \cup (D_1 \cap D'_3)} B(y_E, n_E, p_E | H_a) B(y_C, n_C, p_C | H_a),
 \end{aligned} \tag{1}$$

where  $D_1 = \{(y_E, y_C) : y_E - y_C \geq s\}$ ,  $D_2 = \{(y_E, y_C) : y_E - y_C \leq r\}$ ,  $D_3 = \{y_E : y_E \geq m\}$ . The definition for clinical significance boundary  $m$  remains unchanged. Note that as the difference boundaries change,  $m$  may deviate from what is observed in a 2-by-2 design.

## 2 Tables and figures

Table 1: Determination of  $\gamma_{max}$  and  $\lambda_{max}$  using loss function for TDR one-stage 2-by-2 design at  $p_C = 0.35, p_E = 0.55, \alpha \leq 0.20, \beta \leq 0.20$

| $\pi$ | $N$ | $\gamma_{max}$ | $\lambda_{max}$ | $w_{40}$ | $w_{50}$ | $w_{60}$ |
|-------|-----|----------------|-----------------|----------|----------|----------|
| 0.8   | 56  | 0.01           | 0.05            | 0.44025  | 0.44025  | 0.45621  |
| 0.79  | 56  | 0.02           | 0.1             | 0.44246  | 0.44246  | 0.45807  |
| 0.8   | 46  | 0.03           | 0.1             | 0.41192  | 0.41192  | 0.42038  |
| 0.78  | 42  | 0.05           | 0.15            | 0.40367  | 0.40367  | 0.40872  |
| 0.81  | 40  | 0.07           | 0.15            | 0.39281  | 0.39281  | 0.39727  |
| 0.77  | 38  | 0.1            | 0.2             | 0.39512  | 0.39512  | 0.39685  |

$\gamma_{max}$ : design constraint for  $\gamma$ ;  $\lambda_{max}$ : design constraint for  $\lambda$ ;  $N$ : total sample size;  $\pi$ : power;  $w$ : weight parameter for loss function.

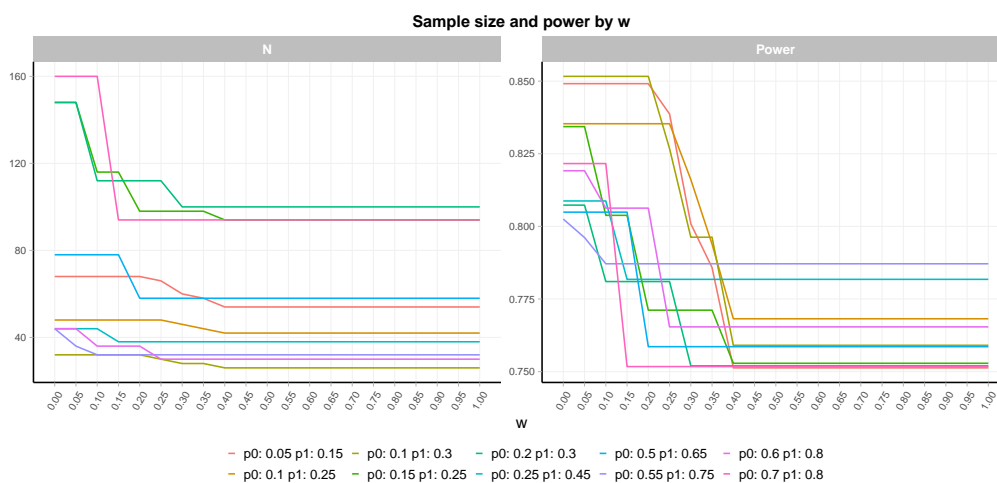


Figure 1: Sensitivity analysis of loss function parameter  $w$ . Ten cases from the one-stage 2-by-2 TDR design were randomly selected to compute loss scores across  $w$ . The optimal sample sizes  $N$  and powers  $\pi$  were plotted.

Table 2: TDR one-stage 2-by-2 design at 30% confidence interval of  $p_C$ ,  $\alpha \leq 0.20, \beta \leq 0.20$

| $p_C$ | $p_E$ | $\gamma_{max}$ | $\lambda_{max}$ | $s$ | $m$ | $N$ | $\pi$ | $\beta$ | $\alpha$ | $\alpha_{max}$ | $\gamma$ | $\eta$ | $\lambda$ |
|-------|-------|----------------|-----------------|-----|-----|-----|-------|---------|----------|----------------|----------|--------|-----------|
| 0.1   | 0.25  | 0.12           | 0.25            | 2   | 4   | 50  | 0.79  | 0.2     | 0.15     | 0.19           | 0.02     | 0.08   | 0.05      |
| 0.1   | 0.3   | 0.08           | 0.2             | 1   | 3   | 28  | 0.8   | 0.13    | 0.14     | 0.2            | 0.08     | 0.23   | 0.15      |
| 0.1   | 0.35  | 0.12           | 0.2             | 1   | 3   | 22  | 0.77  | 0.11    | 0.08     | 0.13           | 0.11     | 0.27   | 0.19      |
| 0.2   | 0.35  | 0.13           | 0.25            | 1   | 9   | 62  | 0.77  | 0.12    | 0.14     | 0.19           | 0.11     | 0.3    | 0.21      |
| 0.2   | 0.4   | 0.1            | 0.15            | 2   | 6   | 40  | 0.77  | 0.19    | 0.14     | 0.19           | 0.04     | 0.13   | 0.09      |
| 0.2   | 0.45  | 0.1            | 0.2             | 1   | 4   | 22  | 0.76  | 0.14    | 0.14     | 0.2            | 0.1      | 0.25   | 0.17      |
| 0.3   | 0.45  | 0.17           | 0.3             | 0   | 14  | 70  | 0.76  | 0.08    | 0.13     | 0.19           | 0.16     | 0.42   | 0.29      |
| 0.3   | 0.5   | 0.12           | 0.25            | 1   | 9   | 42  | 0.77  | 0.12    | 0.13     | 0.19           | 0.11     | 0.3    | 0.21      |
| 0.35  | 0.5   | 0.1            | 0.2             | 2   | 17  | 78  | 0.76  | 0.16    | 0.14     | 0.19           | 0.08     | 0.22   | 0.15      |
| 0.35  | 0.55  | 0.12           | 0.25            | 1   | 11  | 46  | 0.78  | 0.11    | 0.13     | 0.18           | 0.11     | 0.31   | 0.21      |
| 0.35  | 0.6   | 0.1            | 0.15            | 2   | 8   | 32  | 0.77  | 0.18    | 0.12     | 0.16           | 0.05     | 0.17   | 0.11      |
| 0.4   | 0.6   | 0.1            | 0.15            | 2   | 14  | 54  | 0.79  | 0.14    | 0.12     | 0.17           | 0.07     | 0.22   | 0.14      |
| 0.4   | 0.65  | 0.11           | 0.2             | 1   | 8   | 28  | 0.77  | 0.12    | 0.13     | 0.19           | 0.11     | 0.29   | 0.2       |
| 0.5   | 0.65  | 0.1            | 0.2             | 2   | 23  | 78  | 0.76  | 0.16    | 0.14     | 0.19           | 0.08     | 0.23   | 0.15      |
| 0.5   | 0.7   | 0.1            | 0.15            | 2   | 14  | 46  | 0.78  | 0.17    | 0.15     | 0.2            | 0.05     | 0.18   | 0.11      |
| 0.55  | 0.7   | 0.1            | 0.2             | 2   | 25  | 78  | 0.77  | 0.15    | 0.14     | 0.18           | 0.08     | 0.23   | 0.16      |
| 0.55  | 0.75  | 0.1            | 0.15            | 2   | 14  | 42  | 0.76  | 0.19    | 0.15     | 0.19           | 0.05     | 0.17   | 0.11      |
| 0.6   | 0.85  | 0.1            | 0.1             | 2   | 11  | 30  | 0.81  | 0.17    | 0.15     | 0.19           | 0.02     | 0.14   | 0.08      |
| 0.65  | 0.85  | 0.05           | 0.15            | 2   | 16  | 42  | 0.81  | 0.16    | 0.15     | 0.19           | 0.03     | 0.17   | 0.1       |
| 0.7   | 0.85  | 0.11           | 0.25            | 1   | 21  | 52  | 0.77  | 0.12    | 0.14     | 0.2            | 0.11     | 0.3    | 0.2       |

$\gamma_{max}$ : design constraint for  $\gamma$ ;  $\lambda_{max}$ : design constraint for  $\lambda$ ;  $s$ : statistical difference boundary;  $m$ : clinical relevance boundary;  $N$ : total sample size;  $\pi$ : power;  $\alpha$ : type I error;  $\alpha_{max}$ : maximum type I error at 30% confidence interval of  $p_C$ ;  $\beta$ : type II error;  $\gamma$ : inconclusive probability under  $H_a$ ;  $\eta$ : inconclusive probability under  $H_0$ ;  $\lambda$ : average inconclusive probability under  $H_0$  and  $H_a$ .

Table 3: TDR one-stage 3-by-2 design under  $\alpha \leq 0.20, \beta \leq 0.20$

| $p_C$ | $p_E$ | $\gamma_{max}$ | $\lambda_{max}$ | $r$ | $s$ | $m$ | $N$ | $\pi$ | $\beta$ | $\alpha$ | $\gamma$ | $\eta$ | $\lambda$ |
|-------|-------|----------------|-----------------|-----|-----|-----|-----|-------|---------|----------|----------|--------|-----------|
| 0.1   | 0.25  | 0.13           | 0.2             | -5  | 1   | 4   | 44  | 0.79  | 0.08    | 0.15     | 0.12     | 0.27   | 0.2       |
| 0.1   | 0.3   | 0.12           | 0.2             | -5  | 1   | 3   | 28  | 0.8   | 0.09    | 0.14     | 0.12     | 0.25   | 0.18      |
| 0.1   | 0.35  | 0.14           | 0.25            | -4  | 1   | 3   | 22  | 0.77  | 0.09    | 0.08     | 0.14     | 0.28   | 0.21      |
| 0.2   | 0.35  | 0.15           | 0.25            | -7  | 1   | 8   | 56  | 0.77  | 0.08    | 0.16     | 0.14     | 0.3    | 0.22      |
| 0.2   | 0.4   | 0.14           | 0.25            | -6  | 1   | 5   | 32  | 0.78  | 0.09    | 0.17     | 0.13     | 0.27   | 0.2       |
| 0.2   | 0.45  | 0.17           | 0.2             | -5  | 1   | 4   | 24  | 0.81  | 0.07    | 0.17     | 0.12     | 0.26   | 0.19      |
| 0.3   | 0.45  | 0.15           | 0.25            | -8  | 1   | 11  | 58  | 0.77  | 0.09    | 0.2      | 0.14     | 0.28   | 0.21      |
| 0.3   | 0.5   | 0.15           | 0.25            | -6  | 1   | 7   | 34  | 0.77  | 0.09    | 0.19     | 0.14     | 0.27   | 0.21      |
| 0.35  | 0.5   | 0.15           | 0.25            | -8  | 1   | 13  | 60  | 0.76  | 0.09    | 0.19     | 0.15     | 0.29   | 0.22      |
| 0.35  | 0.55  | 0.13           | 0.2             | -7  | 1   | 9   | 40  | 0.81  | 0.07    | 0.2      | 0.12     | 0.27   | 0.2       |
| 0.35  | 0.6   | 0.14           | 0.25            | -5  | 1   | 6   | 24  | 0.78  | 0.08    | 0.18     | 0.14     | 0.27   | 0.2       |
| 0.4   | 0.6   | 0.16           | 0.25            | -7  | 1   | 10  | 38  | 0.76  | 0.09    | 0.16     | 0.15     | 0.3    | 0.22      |
| 0.4   | 0.65  | 0.13           | 0.2             | -5  | 1   | 7   | 26  | 0.81  | 0.07    | 0.19     | 0.13     | 0.27   | 0.2       |
| 0.5   | 0.65  | 0.15           | 0.25            | -9  | 1   | 20  | 68  | 0.78  | 0.08    | 0.17     | 0.15     | 0.31   | 0.23      |
| 0.5   | 0.7   | 0.16           | 0.25            | -6  | 1   | 12  | 38  | 0.77  | 0.08    | 0.16     | 0.15     | 0.3    | 0.23      |
| 0.55  | 0.7   | 0.15           | 0.25            | -8  | 1   | 19  | 60  | 0.78  | 0.08    | 0.2      | 0.14     | 0.29   | 0.21      |
| 0.55  | 0.75  | 0.15           | 0.25            | -6  | 1   | 12  | 36  | 0.8   | 0.07    | 0.19     | 0.13     | 0.28   | 0.21      |
| 0.6   | 0.85  | 0.16           | 0.25            | -4  | 1   | 7   | 18  | 0.77  | 0.08    | 0.19     | 0.15     | 0.26   | 0.2       |
| 0.65  | 0.85  | 0.15           | 0.25            | -5  | 1   | 11  | 28  | 0.78  | 0.07    | 0.18     | 0.15     | 0.27   | 0.21      |
| 0.7   | 0.85  | 0.17           | 0.25            | -6  | 1   | 19  | 48  | 0.79  | 0.07    | 0.19     | 0.14     | 0.28   | 0.21      |

$\gamma_{max}$ : design constraint for  $\gamma$ ;  $\lambda_{max}$ : design constraint for  $\lambda$ ;  $r$ : lower statistical difference boundary;  $s$ : upper statistical difference boundary;  $m$ : clinical relevance boundary;  $N$ : total sample size;  $\pi$ : power;  $\alpha$ : type I error;  $\beta$ : type II error;  $\gamma$ : inconclusive probability under  $H_a$ ;  $\eta$ : inconclusive probability under  $H_0$ ;  $\lambda$ : average inconclusive probability under  $H_0$  and  $H_a$ .

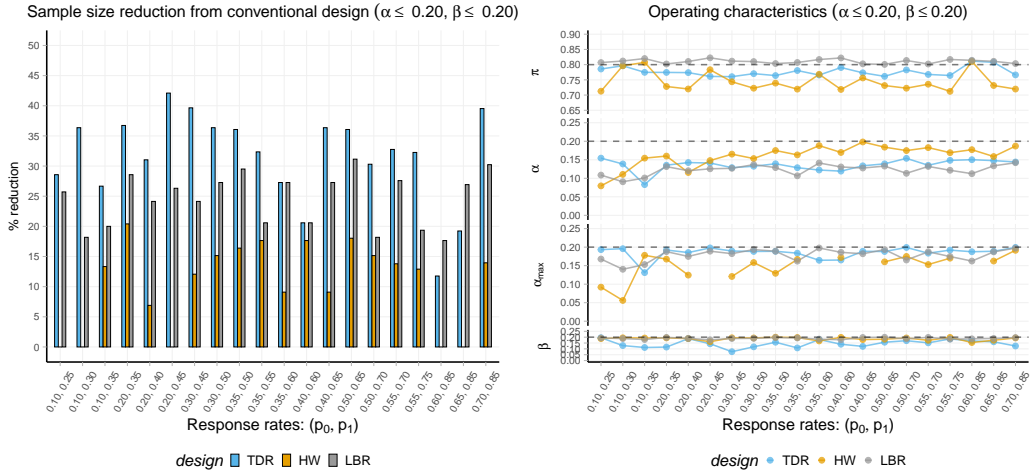


Figure 2: Robustness of the one-stage 2-by-2 TDR design at 30% confidence interval of  $p_C$ . (a) Sample size reduction with respect to the two-sample  $t$ -test at 30% confidence interval of  $p_C$ ; (b) Operating characteristics power  $\pi$ , type I error  $\alpha$ , maximum type I error  $\alpha_{max}$  at 30% confidence interval of  $p_C$ , and type II error  $\beta$ .

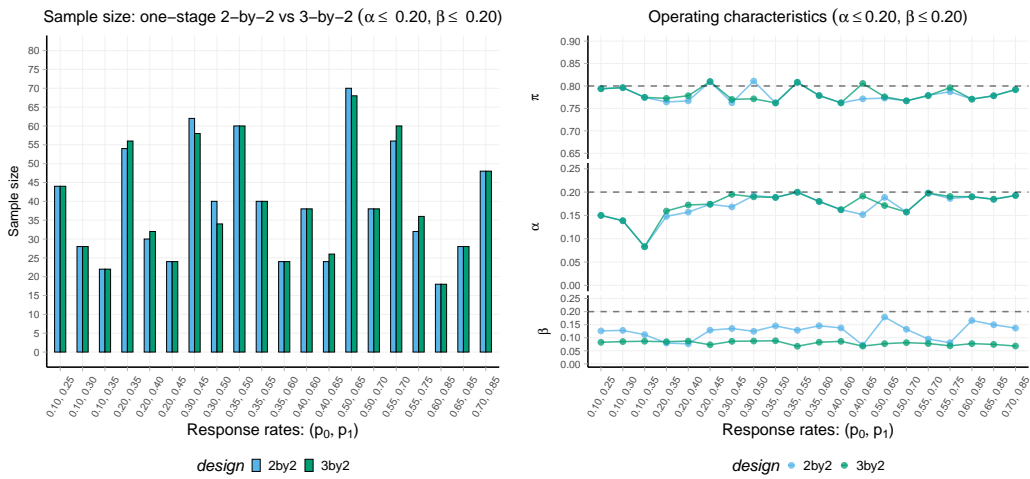


Figure 3: Comparison of one-stage 2-by-2 TDR design with 3-by-2 TDR design under  $\alpha \leq 0.20, \beta \leq 0.20$ . (a) Sample size reduction with respect to the two-sample  $t$ -test; (b) Operating characteristics power  $\pi$ , type I error  $\alpha$ , and type II error  $\beta$ .